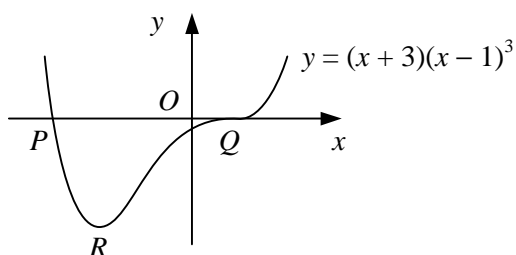


# C3 DIFFERENTIATION

## Worksheet G

- 1 A curve has the equation  $y = x^2(2 - x)^3$  and passes through the point  $A(1, 1)$ .
- Find an equation for the tangent to the curve at  $A$ .
  - Show that the normal to the curve at  $A$  passes through the origin.
- 2 A curve has the equation  $y = \frac{x}{2x+3}$ .
- Find an equation for the tangent to the curve at the point  $P(-1, -1)$ .
  - Find an equation for the normal to the curve at the origin,  $O$ .
  - Find the coordinates of the point where the tangent to the curve at  $P$  meets the normal to the curve at  $O$ .

3



The diagram shows the curve with equation  $y = (x + 3)(x - 1)^3$  which crosses the  $x$ -axis at the points  $P$  and  $Q$  and has a minimum at the point  $R$ .

- Write down the coordinates of  $P$  and  $Q$ .
  - Find the coordinates of  $R$ .
- 4 Given that  $y = x\sqrt{4x+1}$ ,
- show that  $\frac{dy}{dx} = \frac{6x+1}{\sqrt{4x+1}}$ ,
  - solve the equation  $\frac{dy}{dx} - 5y = 0$ .
- 5 A curve has the equation  $y = \frac{2(x-1)}{x^2+3}$  and crosses the  $x$ -axis at the point  $A$ .
- Show that the normal to the curve at  $A$  has the equation  $y = 2 - 2x$ .
  - Find the coordinates of any stationary points on the curve.
- 6  $f(x) \equiv x^{\frac{3}{2}}(x-3)^3, x > 0$ .
- Show that  $f'(x) = kx^{\frac{1}{2}}(x-1)(x-3)^2$ , where  $k$  is a constant to be found.
  - Hence, find the coordinates of the stationary points of the curve  $y = f(x)$ .
- 7  $f(x) = x\sqrt{2x+12}, x \geq -6$ .
- Find  $f'(x)$  and show that  $f''(x) = \frac{3(x+8)}{(2x+12)^{\frac{3}{2}}}$ .
  - Find the coordinates of the turning point of the curve  $y = f(x)$  and determine its nature.